

Computational Analysis of Interacting Web services: a Logical Approach

Philippe Balbiani and Fahima Cheikh

LILaC

Irit

Outline of the talk

- Model for web services
- Web services composition
- Composition problem decidability

Introduction

- Services oriented computing
- What is a Web service ?

Information system

- Structure of the form $IF=(Obj,Att,Val,f)$

- | f | a1 | a2 |
|----|---------|------|
| o1 | {v1,v2} | {} |
| o2 | {v1} | {v3} |

$Val=\{v1,v2,v3,v4,v5\}$

Example

- Information system for manufactured goods.

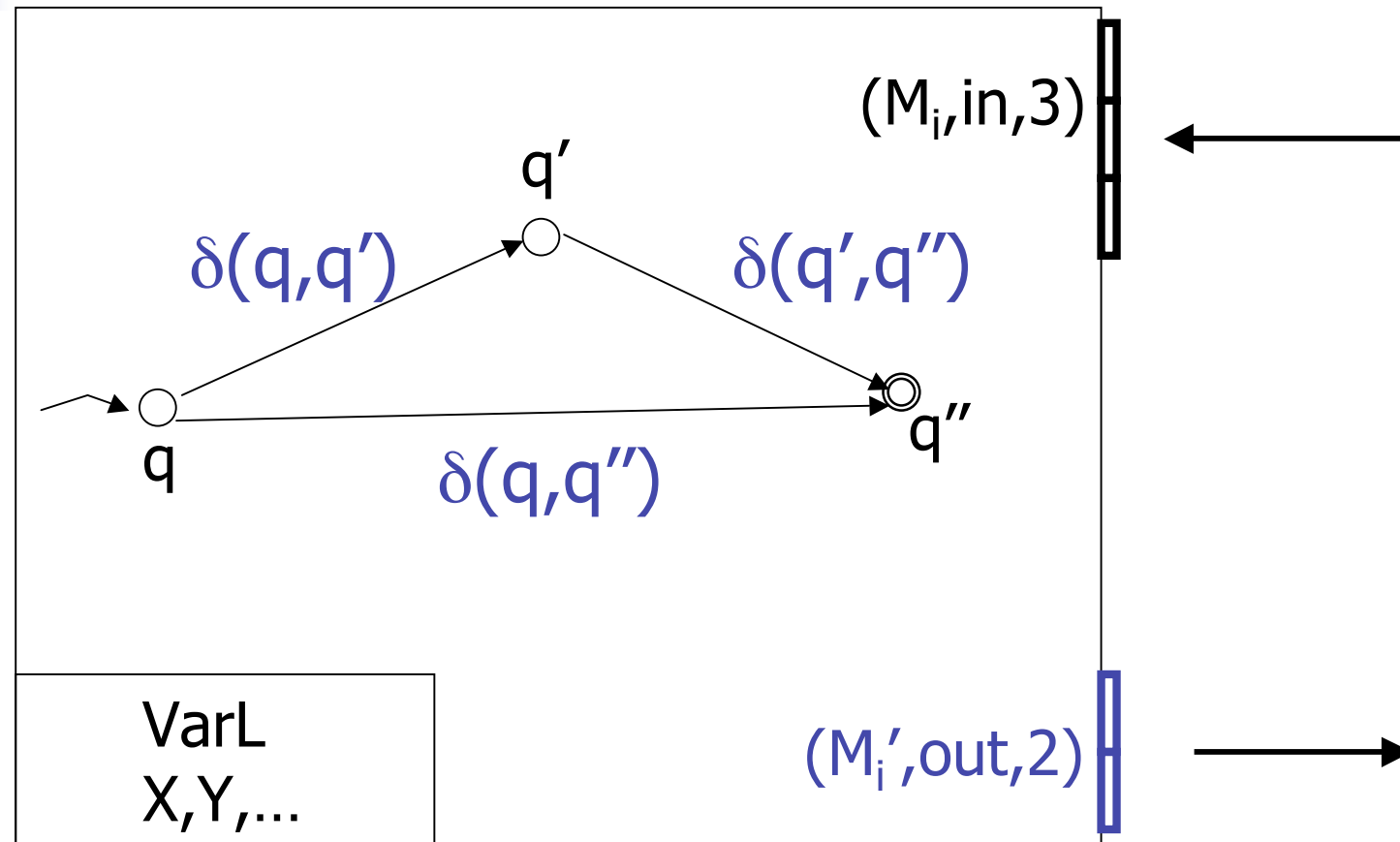
f	name	price	color
o1	{sweater}	{40}	{blue, white}
o2	{skirt}	{80}	{black, white}

Val={sweater, skirt, dress, 40, 80, blue, white, black, red }
5

Web service

- Web service is defined w.r.t. to an information system
- It is a structure of the form $S=(Q,I,F,VarL,P, \delta)$
 - Q: finite set of states
 - I: set of initial states
 - F: set of final states
 - VarL: finite set of local variables
 - P: finite set of ports
 - δ : transition function

Web service



Web service S_i

Web service

- Transition function

$\delta(q, q') = \{(C, \alpha) \mid C \text{ is a condition, } \alpha \text{ is a sequence of primitive operations}\}$

- Condition

$C := T \mid (\theta_1 = \theta_2) \mid (\theta \in f(z, a)) \mid \neg C \mid (C_1 \wedge C_2) \mid \exists z C$

θ : local variable or a value in Val

z : variable ranging over Obj

a : attribute in Att

Web service

- primitive operations

- create object Z
- destroy object z
- add θ to $f(z,a)$
- delete θ from $f(z,a)$



IF update

- $x := \theta$

allocate a value

- $?M(\theta_1, \dots, \theta_n)$

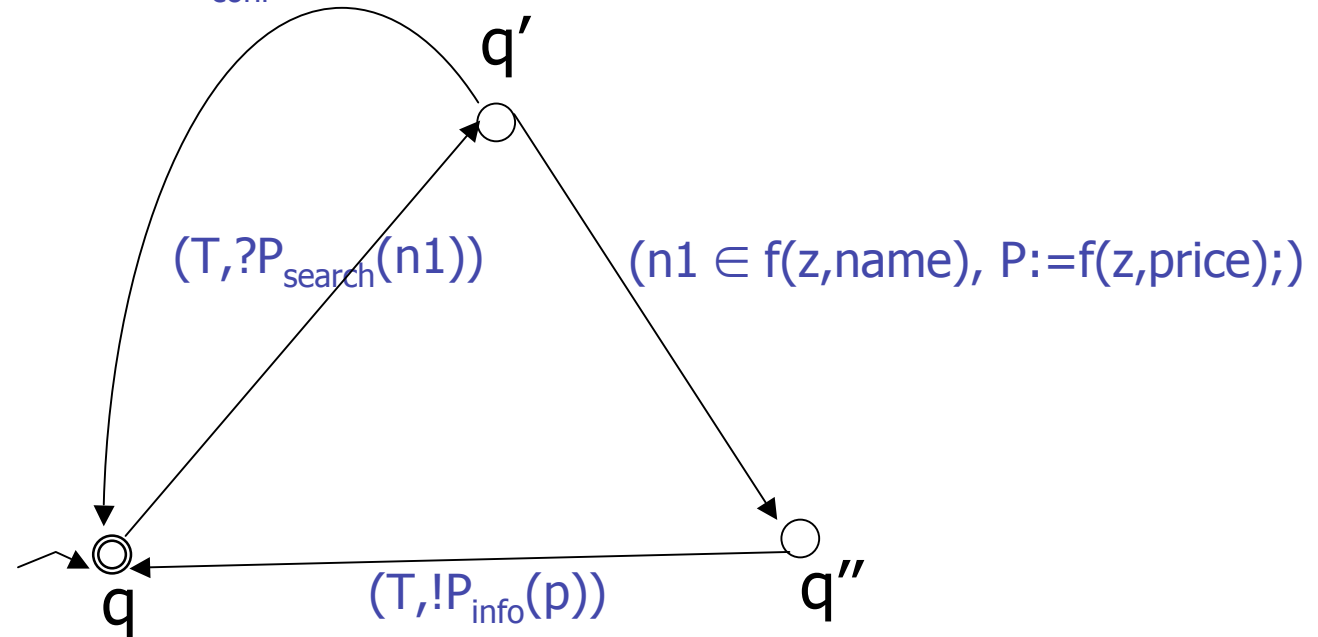
receive a message

- $!M'(\theta_1, \dots, \theta_m)$

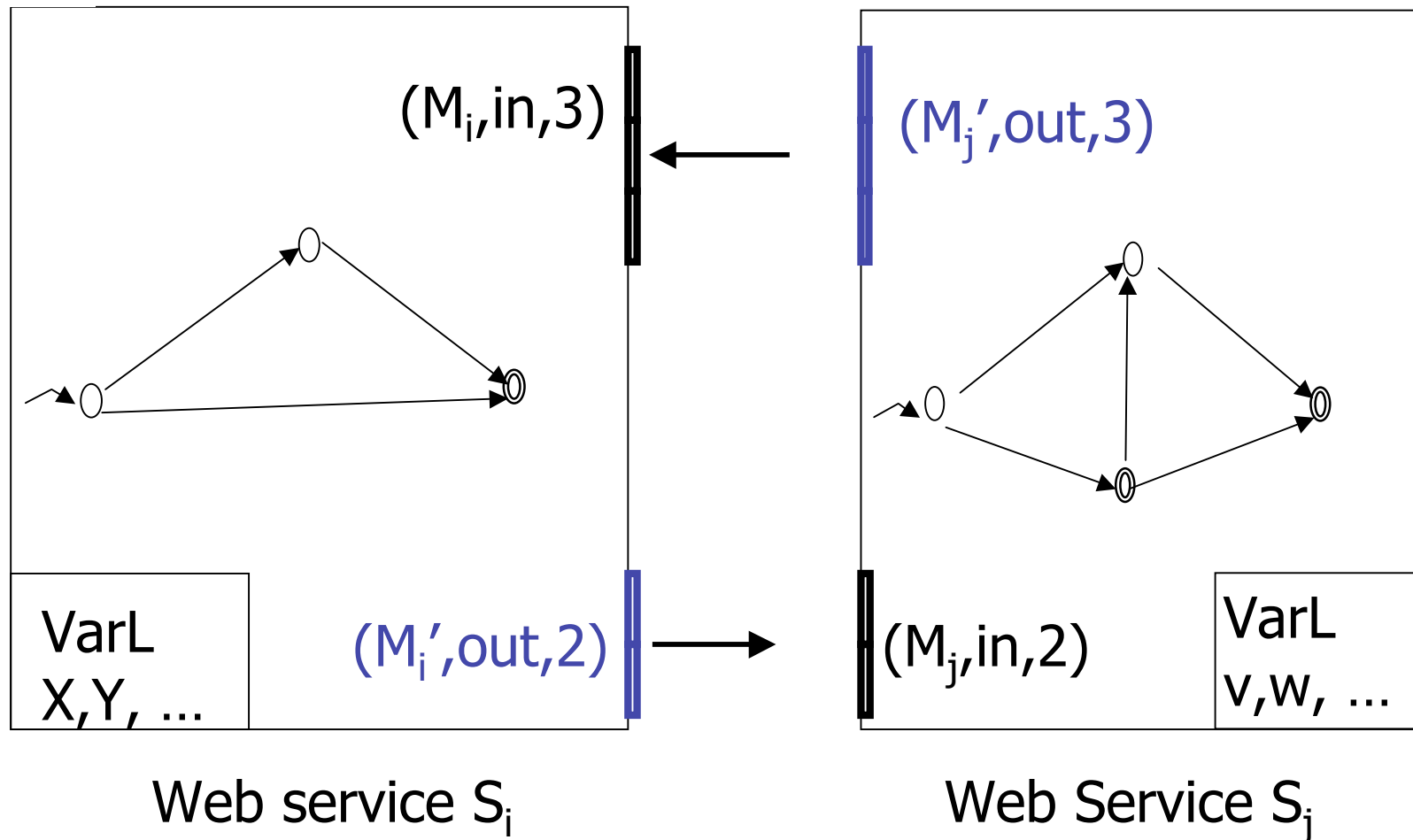
send a message

Example

$(\forall z(n1 \notin f(z, name)), !P_{\text{conf}}(\text{failure}))$



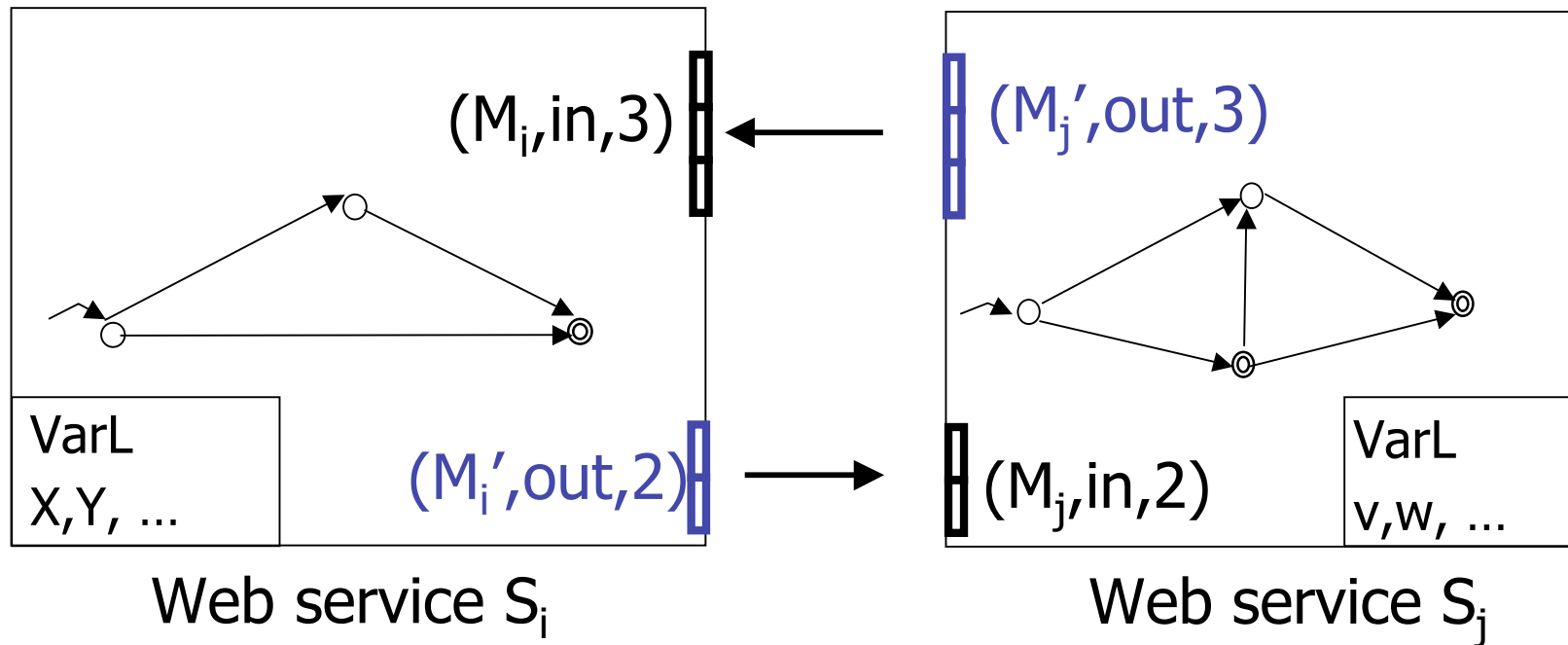
Web service



Link

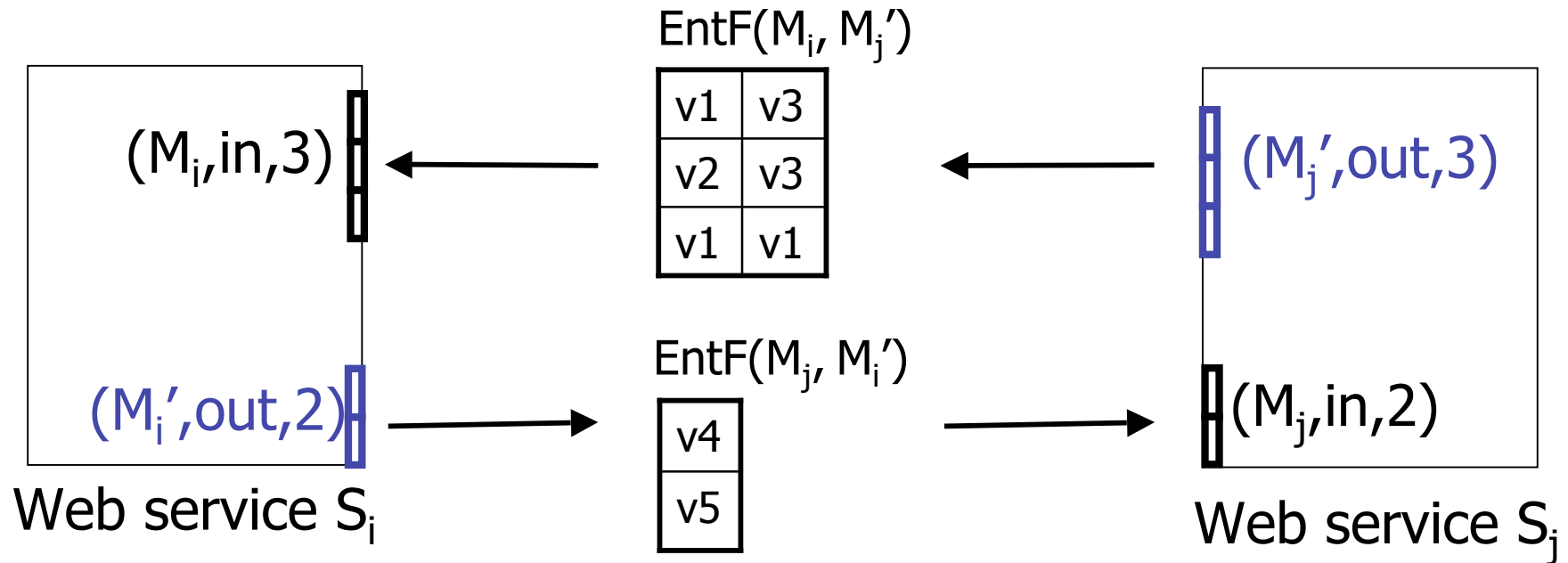
- $C = \{S_0, \dots, S_n\}$ set of services
- $P_i, i \in \{0, \dots, n\}$ set of S_i ports
- A **C-link** L is a binary relation on $P_0 \cup P_1 \cup \dots \cup P_n$
- L is defined such that:
 - if $(M, d, m) L (M', d', m')$ then $d = \text{in}, d' = \text{out}, m = m'$
 - if $(M, d, m) L (M', d', m')$ and $(M, d, m) L (M'', d'', m'')$ then $M' = M''$
 - if $(M, d, m) L (M'', d'', m'')$ and $(M', d', m') L (M'', d'', m'')$ then $M = M'$

Example



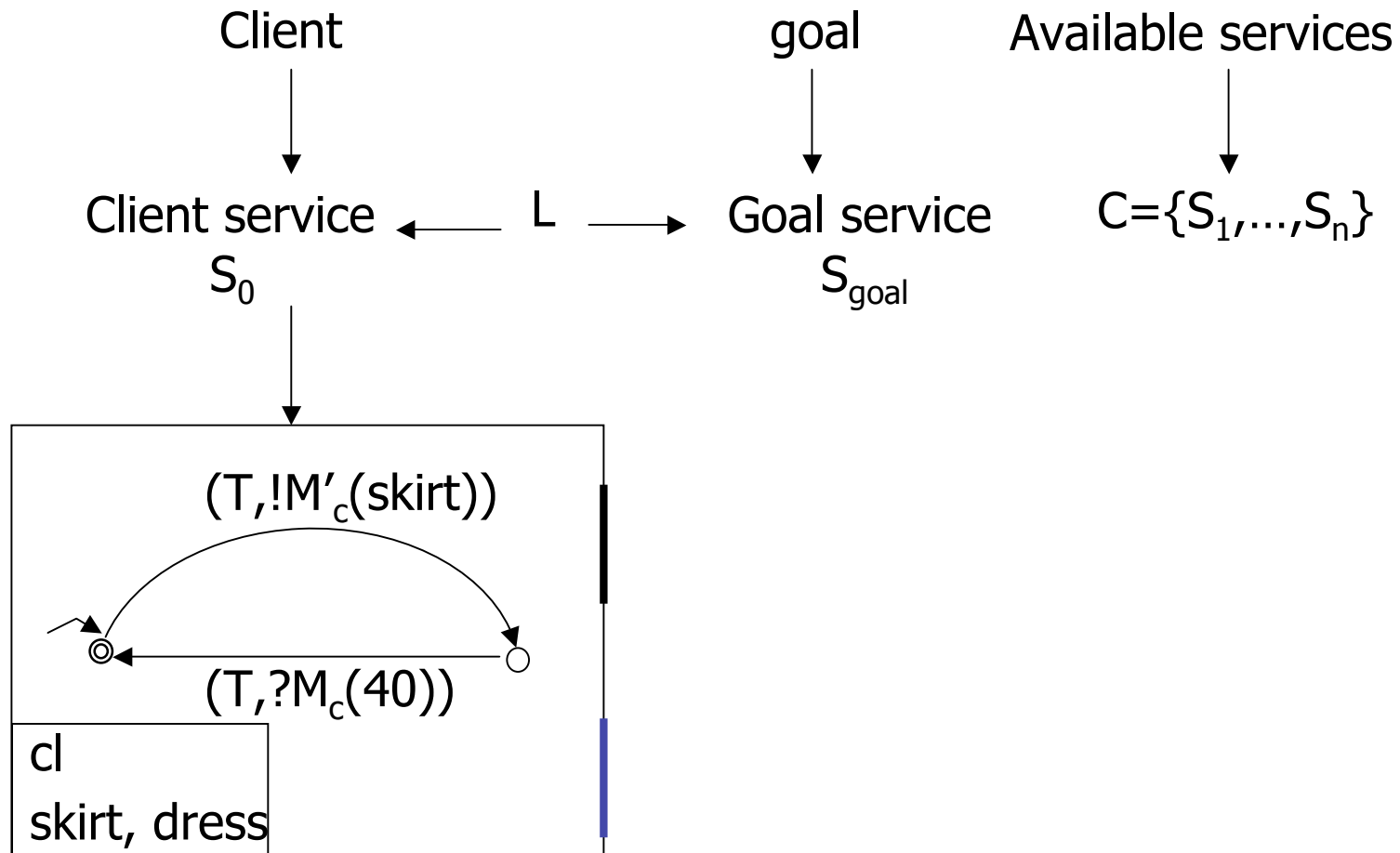
- $L = \{(M_i, M_j'), (M_j, M_i')\}$

Queue

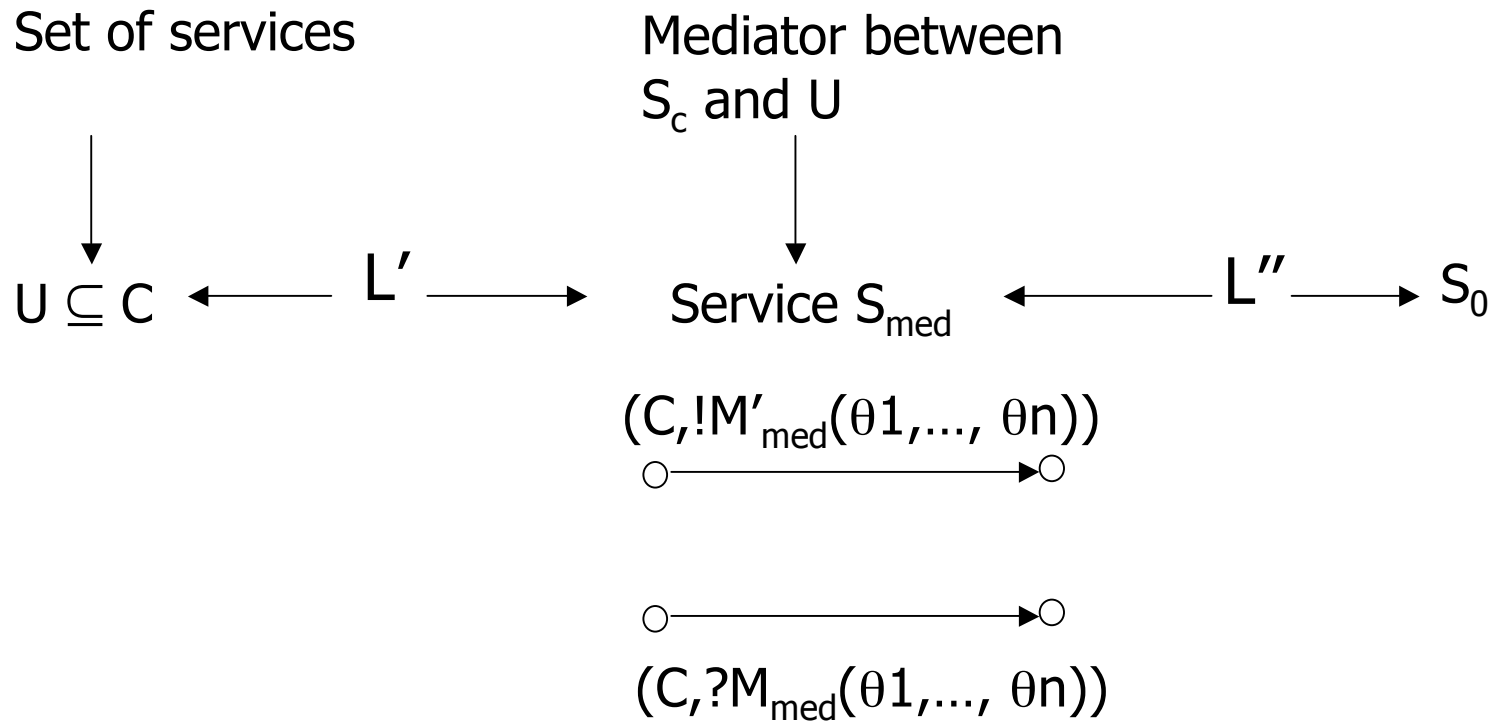


What is the composition
problem?

Input



Output



➤ The behavior of $\{S_0, S_{\text{med}}, U\}$ is equivalent to that of $\{S_0, S_{\text{goal}}\}$

Nodes

- A node, in a tree for $C = \{S_0, \dots, S_n\}$ and a C-link L , is a structure of the form

$$\Delta = (\text{IF}, q_0, \dots, q_n, \text{int}_0, \dots, \text{int}_n, \text{EntF}, \text{cl})$$

- IF: information system
- q_i : state of S_i
- $\text{int}_i: \text{Var}L_i \rightarrow \text{Val}$
- EntF: $(M, M') \in L \rightarrow \text{EntF}(M, M')$
- cl: finite set of values

Edges

○ $(IF, q_0, \dots, q_i, \dots, q_n, int_0, \dots, int_i, \dots, int_n, EntF, cl)$

α

▼ ○ $(IF', q_0, \dots, q'_i, \dots, q_n, int_0, \dots, int'_i, \dots, int_n, EntF, cl)$

○ $(IF, q_0, \dots, q_i, \dots, q_n, int_0, \dots, int_i, \dots, int_n, EntF, cl)$

?M($\theta_1, \dots, \theta_m$)

$EntF(M, M') \neq \emptyset$
 $(M, M') \in L$

▼ ○ $(IF, q_0, \dots, q'_i, \dots, q_n, int_0, \dots, int'_i, \dots, int_n, EntF', cl)$

Equivalence between trees

- Two trees T and T' are embedding equivalent if T is included in T'
- Two trees T and T' are weakly equivalent if T and T' are similar

Composition problem

- Input: client service S_0 , goal service S_{goal} , link L for S_0 and S_{goal} , and finite set $C = \{S_1, \dots, S_n\}$
- Output: determines if there exists a subset U of C , a mediator service S_{med} , a link L' for S_{med} and S_0 and, a link L'' for S_{med} and U such that:
 - ∀ IF tree($S_0, S_{\text{goal}}, L, \text{IF}$) is embedding (resp. weakly) equivalent to tree ($S_0, S_{\text{med}}, L', U, L'', \text{IF}$)

Decidability

- Theorem 1

The embedding composition problem is undecidable

Proof. We reduce the uniform halting problem of Minsky machines to the embedding composition problem

Decidability

- Theorem 2

The weakly composition problem is undecidable

Proof. We reduce the 0-halting problem of Minsky machines to the weakly composition problem

Decidability

Some restrictions:

- There is no condition in the transitions
- Queues' length is limited to at most 1 message
- Service mediator has at most k states and b ports

Decidability

- Theorem 3

The weakly composition problem is decidable, when restrictions above are considered

Proof. 1- The number of all possible U , S_{med} L' and L'' is bounded and countable

2- $L(T)$ and $L(T')$ are rational

Conclusion

- Composition problem decidability
- Services and safety policies
- Services and cryptographic protocols